

Thu 30 Jan

41 97 14

Random walk example in money space - roulette

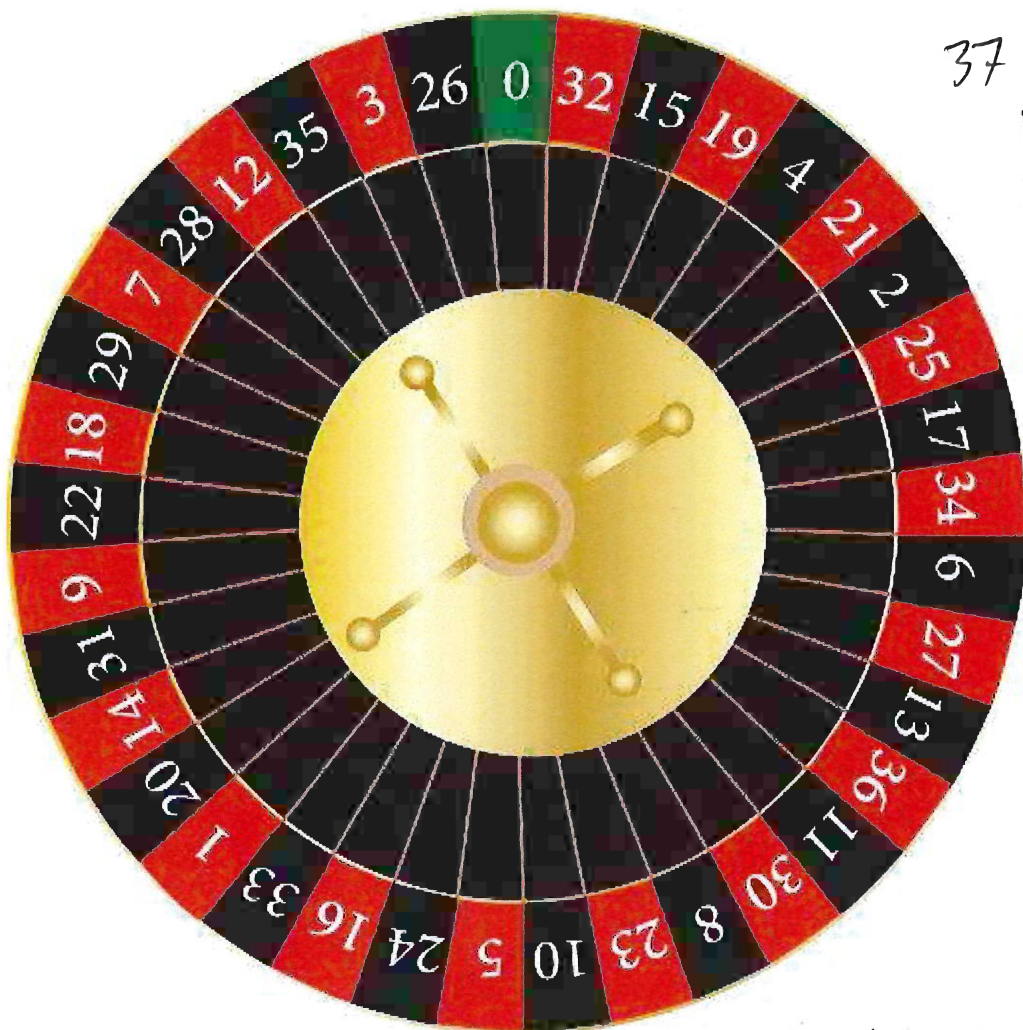
Three different ways of computing probabilities

Direct "brute force"

Central limit theorem

Simplified approximation

(numerical integration)



37 pockets
18 red
18 black
1 green

\mathcal{E} : Spin wheel

X : Measure pocket #/colour

$$A = \{0, 1, 2, \dots, 36\}$$

"Fair" wheel

$$p = 1/37$$

$$\mathcal{F} = A$$

$$\begin{aligned} P(A) &= P(0 \text{ or } 1 \text{ or } \dots \text{ or } 36) \\ &= P_0 + P_1 + \dots + P_{36} = 37p = 1 \end{aligned}$$

Game

Event $\mathcal{F} = \{ \text{red, black, green} \}$

Place £5 bet on black

Win: get back £10

Lose: get back £0

page 13

$$P_{\text{win}} = 18/37 = P_{\text{red}}$$

$$P_{\text{lose}} = 1 - P_{\text{win}} = 19/37$$

$$= 18/37 + 1/37 = P_{\text{black}} + P_{\text{green}}$$

$G_{\text{win}} = +5$

$G_{\text{lose}} = -5$

Gain G : Money we back minus money we spend
(can be negative)

$G(N, w) = 10w - 5N$

$P_w = \binom{N}{w} P_{\text{win}}^w P_{\text{lose}}^{N-w} = \binom{N}{w} \frac{18^w 19^{N-w}}{37^N}$

$N=5$
 $P_0 = \binom{5}{0} \left(\frac{19}{37}\right)^5 \approx 0.036$

$P_1 = \dots$

$P_2 = \dots$

$P_3 = \binom{5}{3} \frac{18^3 19^2}{37^5} = 10 \frac{18^3 19^2}{37^5} \approx 0.304$

$P_4 = \dots$

$P_5 = \dots$

Automate!