

Statistical Physics 2019/20  
MATH327  
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Computer project generic feedback & any requests

Monday 11 May

## Computer project Part B feedback

Little trouble with Exercise 4, Exercise 5 more challenging

One challenge was how to check results (e.g., dependence of  $\alpha$  on  $\theta$ )  
without exact knowledge based on the central limit theorem

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**Useful check:** We know ordinary diffusion ( $l_\theta \propto N^{1/2}$  with  $\alpha = 1/2$ )  
only possible if single-step standard deviation  $\sigma$  exists

We know  $\sigma$  does not exist for the Cauchy–Lorentz distribution

$\implies$  should be no chance of  $\alpha = 1/2$  for **any**  $\theta$

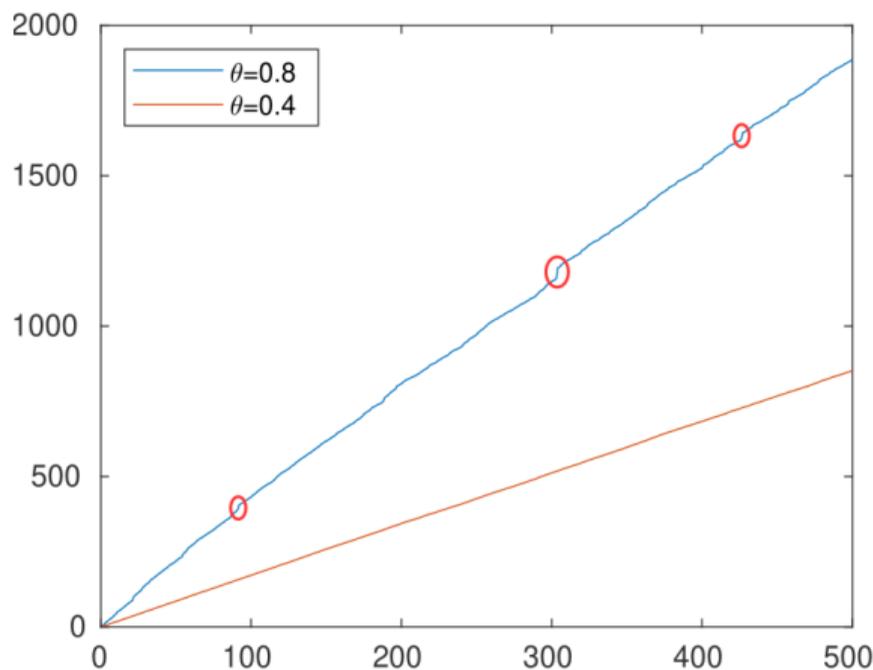
## $\theta$ dependence more generally

$\alpha = 1$  independent of  $\theta$

But random fluctuations increase with  $\theta$   
(big steps from fat tails less suppressed)

→ More chance of  $\alpha$  farther from 1

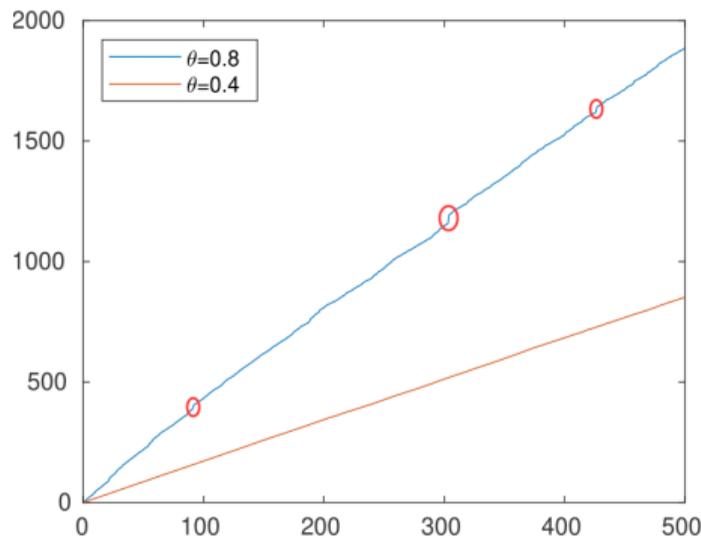
$\alpha_{0.8} \approx 0.9526$       vs.       $\alpha_{0.4} \approx 0.9987$



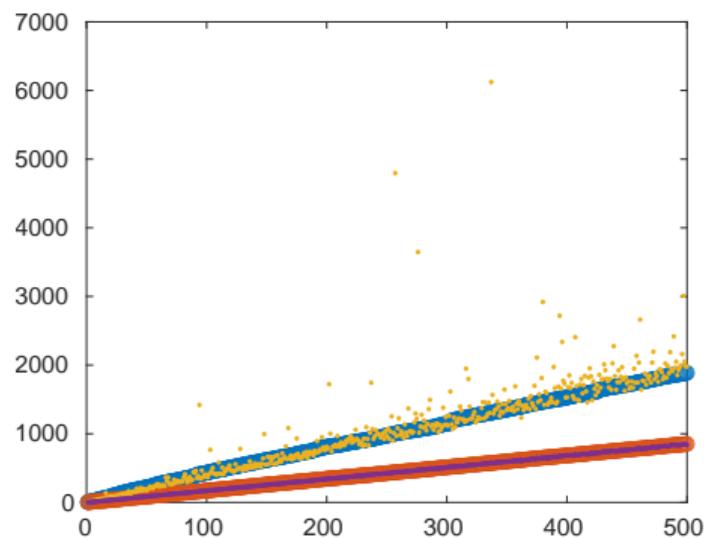
Issue easier to see with 500 independent (rather than correlated) walks...

## $\theta$ dependence more generally

$$\alpha_{0.8} \approx 0.9526 \quad \text{vs.} \quad \alpha_{0.4} \approx 0.9987$$

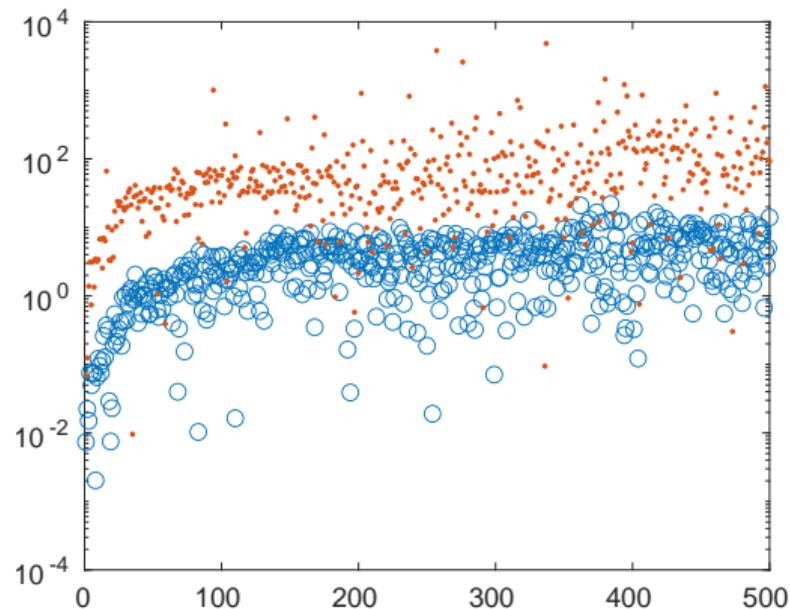
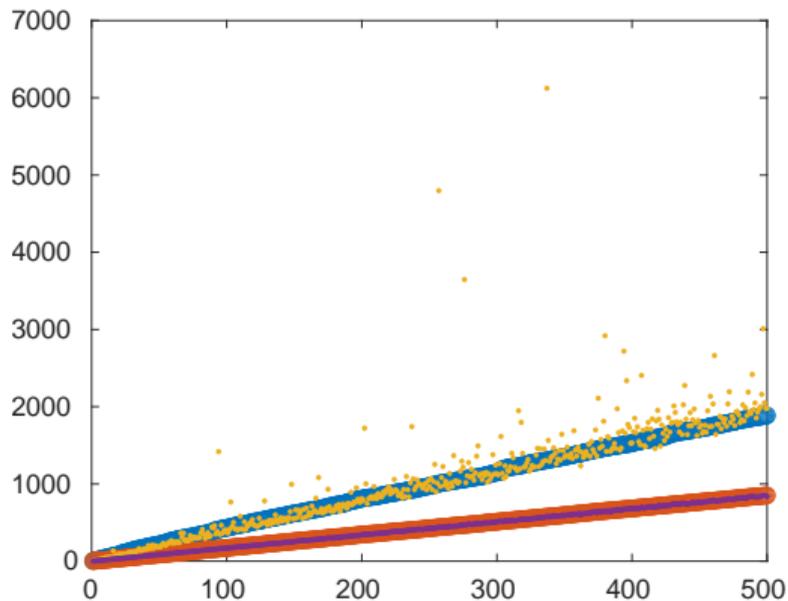


$$\alpha_{0.8} \approx 1.0064 \quad \text{vs.} \quad \alpha_{0.4} \approx 1.0001$$



More random samples  $\longrightarrow$  more big steps,  
though for  $\theta < 1$  statistics will (eventually) win

## $\theta$ dependence more generally



Fit residuals roughly double for  $\theta = 0.4$  (same as for ordinary diffusion)  
vs. much larger  $\sim 5\times$  increase for  $\theta = 0.8$

## Request: Extra practice problems

### **EXTRA 1:** Entropies and probabilities from rolling dice



## Request: Extra practice problems

More possibilities in [David Tong's problem sheets](#), including the following:

**EXTRA 2:** Fugacity and particle number fluctuations  
in the grand-canonical ensemble

**EXTRA 3:** Internal energy and average occupation numbers  
for non-interacting fermions in the grand-canonical ensemble

**EXTRA 4:** The  $q$ -state Potts model as a generalization of the Ising model

Can also provide digital copy of Schroeder's textbook, with many exercises